

## APPLICATION PERTURBATION THEORY FOR CALCULATION OF THE THERMODYNAMIC PROPERTIES OF METALS

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**Abstract:** Application of the equation of state based on perturbation theory is demonstrated on calculating the properties of condensed aluminum and copper during isothermal compression. For a description of intermolecular interactions in metals, Morse pair potential is used. The calculation results are in good agreement with experimental data and calculations based on the described in the literature empirical and analytical equations of state. Thus, the equation of state developed on the basis of perturbation theory and using the corresponding intermolecular interaction potential is a reliable universal tool for the calculation of the thermodynamic properties of gas (fluid) systems and condensed matter physics and allows one to analyze changes in the atomic structure of the matter.

**Keywords:** perturbation theory; intermolecular interaction potential Morse; thermodynamic parameters of state; radial distribution function; isothermal compression

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